

# Prognostische Modelle in der klinischen Forschung – Ein Blick in die Glaskugel

DCR-CTU lecture

**André Moser, Senior Statistician, CTU Bern**

[andre.moser@ctu.unibe.ch](mailto:andre.moser@ctu.unibe.ch)

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In this DCR-CTU lecture we dare a look into the crystal ball and discuss **some key elements** of prognostic modelling from a **regression modeling perspective**.

**No (or hopefully less) crystal ball anymore** 🎮

# Premise of prognostic models in clinical research

Prognostic models are tools

- (shared) **decision making** between patients and clinicians
- a better understanding of **disease determinants**
- **health economic evaluation** and **benchmarking**
- which are **communicable, implementable** and **reproducible**

## **Development phase**

Prognosis aim, study outcomes, study design, candidate predictor selection, statistical model

## **Validation phase**

Performance assessment and internal validation  
Performance in new patients (external validation)

## **Impact phase**

Does the model improve decision making and patient outcomes?

# Development phase



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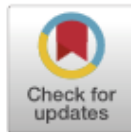
# Study aim for clinical prediction models

*u*<sup>b</sup>

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Journal of  
Clinical  
Epidemiology

## ORIGINAL ARTICLE

### Mortality prediction in intensive care units including pre-morbid functional status improved performance and internal validity

André Moser<sup>a,\*</sup>, Matti Reinikainen<sup>b</sup>, Stephan M. Jakob<sup>c</sup>, Tuomas Selander<sup>d</sup>, Ville Pettilä<sup>e</sup>,  
Olli Kiiski<sup>f</sup>, Tero Varpula<sup>g</sup>, Rahul Raj<sup>h,1</sup>, Jukka Takala<sup>c,1</sup>

<sup>a</sup> CTU Bern, University of Bern, Mittelstrasse 43, 3012 Bern, Switzerland

<sup>b</sup> Department of Anaesthesiology and Intensive Care, Kuopio University Hospital and University of Eastern Finland, Kuopio, Finland

<sup>c</sup> Department of Intensive Care Medicine, Bern University Hospital, University of Bern, Bern, Switzerland

<sup>d</sup> Science Service Center, Kuopio University Hospital, Kuopio, Finland

<sup>e</sup> Division of Intensive Care, University of Helsinki and Helsinki University Hospital, Helsinki, Finland

<sup>f</sup> Health and Care, Benchmarking Services, TietoEvy, Helsinki, Finland

<sup>g</sup> Division of Intensive Care, University of Helsinki and Helsinki University Hospital, Helsinki, Finland

<sup>h</sup> Department of Neurosurgery, University of Helsinki and Helsinki University Hospital, Helsinki, Finland

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# Study aim for clinical prediction models

**Clinical practice:** Diagnosis, clinical decision making

**Economic evaluation:** Benchmarking

**Public health:** Preventive interventions

**Research:** Inclusion in RCTs

**Study population, outcomes and candidate predictors are  
tailored to the prognosis aim.**

# Study design



<b>Design</b>	<b>Example</b>	<b>Pros</b>	<b>Cons</b>
<b>Prospective designs</b>	Multicenter RCTs	Data quality	Generalizability
<b>Retrospective design</b>	Patient records	Simple, costs	Patient selection
<b>Registries</b>	Cancer / Insurance	Large, coverage	Outcome assessment
<b>Case-control</b>	Rare diseases	Simple, costs	Choice of controls



**Dear Statistician.**

**I want to develop a prediction model, how much patients do I need?**

- Often used **rule of thumb** «10 events per variable (EPV)» is too simple (doi: 10.1177/0962280218784726)

- Sample size depends on more: For example, outcome proportion and expected predictive performance

- Guidelines

**Riley et al.** Calculating the sample size required for developing a clinical prediction model (doi: 10.1136/bmj.m441)

**Or ask your statistician of trust at CTU Bern for support!**

# Candidate predictor selection



*«Ideally, candidate predictors are selected without studying the predictor-outcome relationship in the data under study.»*

***Steyerberg, Clinical Prediction Models, Springer***

**Good starting point:**

Choose 5-20 predictors based on literature and expert knowledge

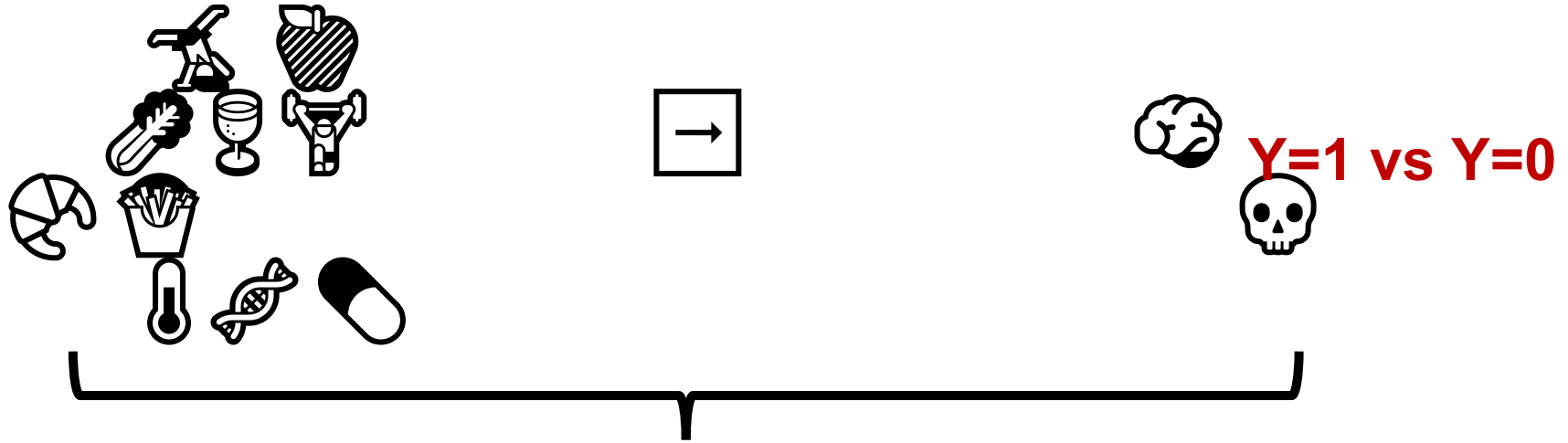
# 'Automated' predictor selection



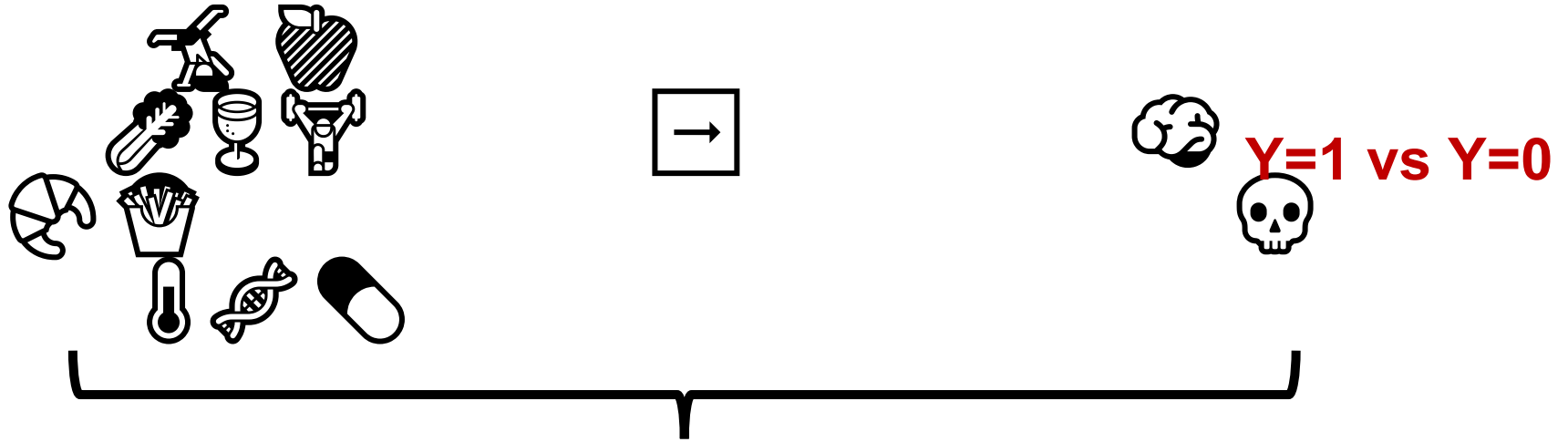
'Statistical' selection procedures: **Doable, but...**

- introduce '**variable selection bias**' based on arbitrary cut-offs ( $p < 0.05$ )
- might lead to **biased coefficients**
- moves towards an **estimation** problem for exploration, not a prediction problem

**Depends** study aim and context (e.g. large studies)!



**Multivariable prediction model  
(here: binary outcome)**



**Multivariable prediction model  
(here: binary outcome)**



# Statisticians at work!



# Output from statistical model

Observed outcome

$P(Y=1)$

	X		0.219
	X		0.550
 			0.604
			0.346
	X		0.010

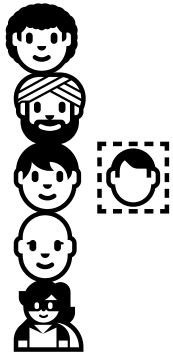
# Validation phase



# Validation

Observed death

$P(Y=1)$



Good/poor?



0.219

0.550

0.604

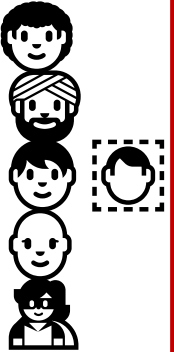




0.346

0.010

# Terminology: Optimism

Observed death

$P(Y=1)$

		$P(Y=1)$
		0.219
		0.550
		0.604
		0.346
	<b>Development sample</b>	0.010
		



**True population**

Too optimistic estimates?  
“What you see may not be what you get.”

- **Optimism:** True performance vs development performance (**internal validation process**)
- Overfitting is a statistical problem which occurs when **too many variables** are fitted in a model with **too few events**
- Overfitting leads to optimism
- **Internal validation** and “**shrinkage methods**” try to minimize optimism

## Validation phase

### Internal validation:

Optimism  
Bootstrapping  
Cross validation  
Shrinkage

### Performance assessment:

Overall performance  
Discrimination  
Calibration

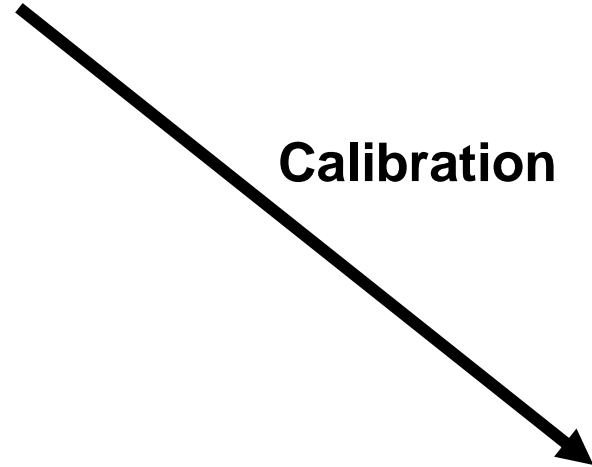
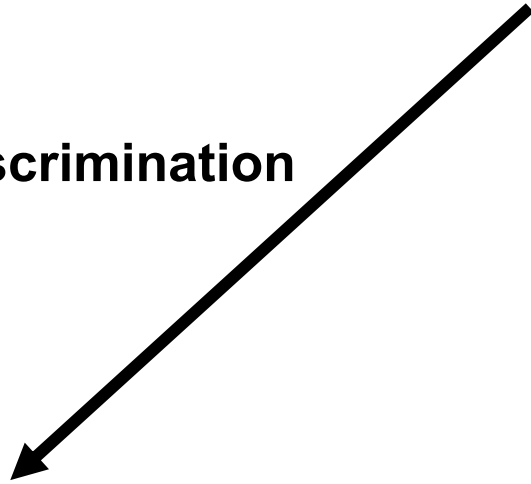
### External validation:

Performance in new  
patients?  
Performance in different  
centers/periods?

Performance assessment

**Discrimination**

**Calibration**

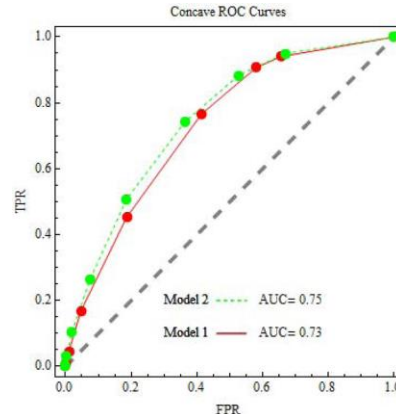


Distinction between individuals  
with and without event

Observed vs predict event rates



- AUC=area under receiver operating characteristics curve
- Binary outcomes: **c-statistic=AUC**
- A value between **0.5** (uninformative model, coin flip) and **1** (perfect discrimination)



Source: doi: 10.1002/sim.6195

# Levels of calibration

## Level 1

Mean

## Level 2

Weak

## Level 3

Moderate

## Level 4

Strong

Over- or underestimation  
of risk?

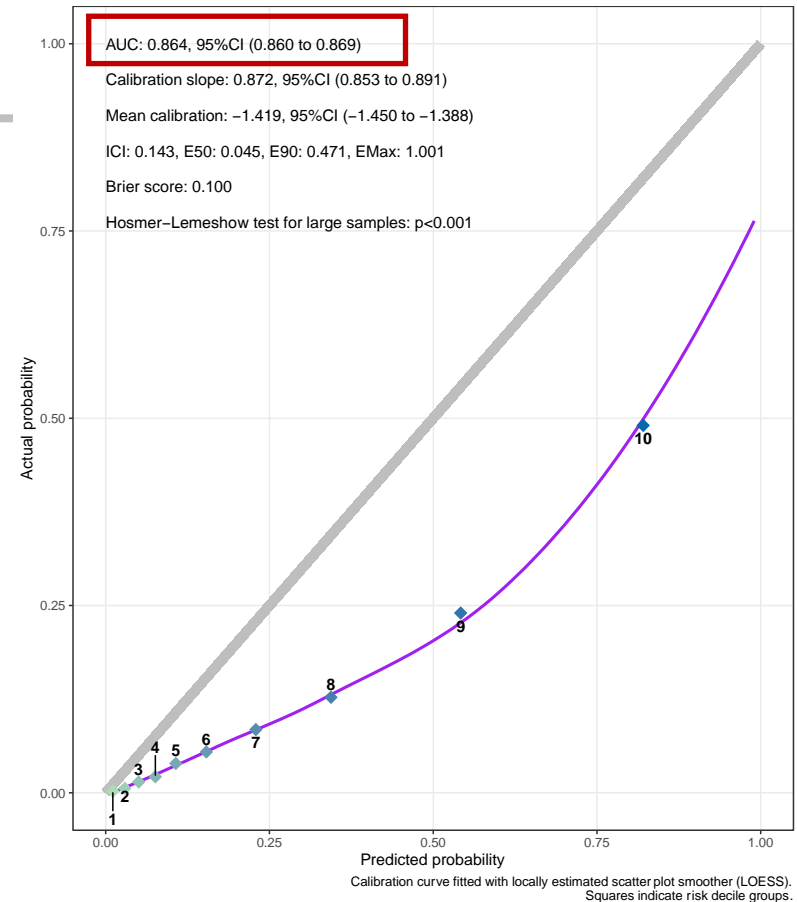
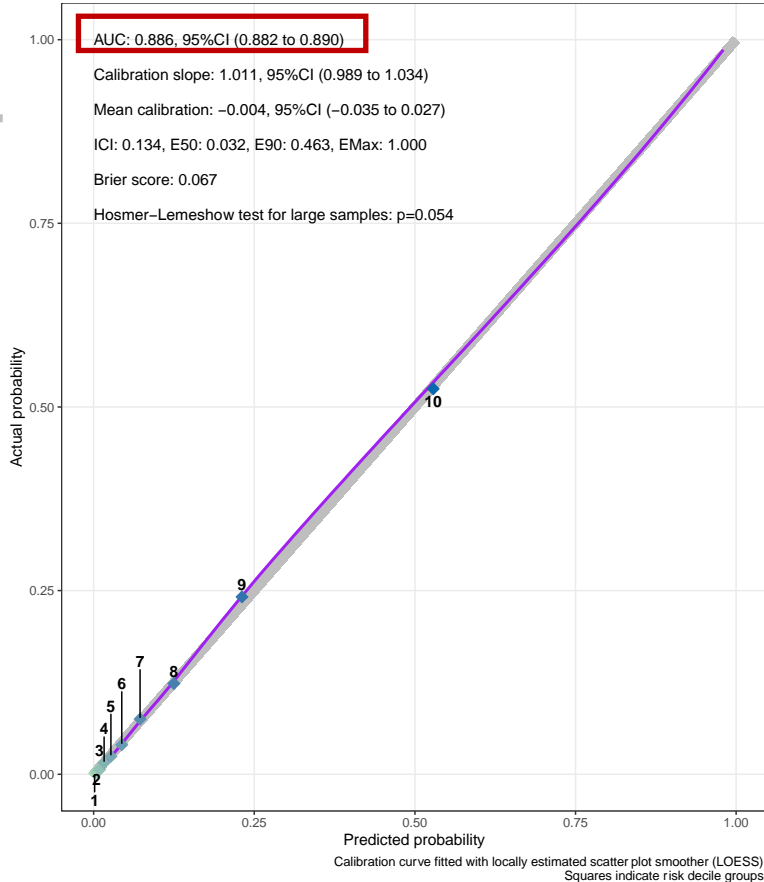
Predicted risks  
correspond  
to observed  
event rate?

Predicted risks  
correspond  
to observed  
event rate **among all  
covariate patterns**

Observed event rate equals  
**average** predicted risk?

# Discrimination and calibration

$u^b$

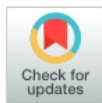


# The myth about data splitting for ‘validation’

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## COMMENTARY

### Validation in prediction research: the waste by data splitting

Ewout W. Steyerberg<sup>a,b,\*</sup>

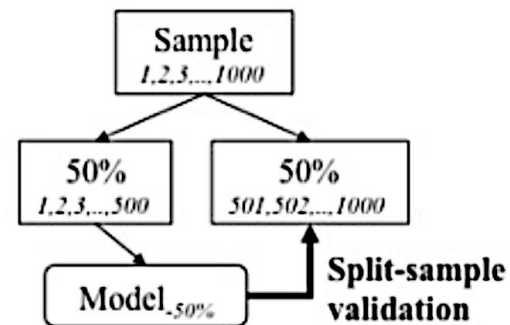
<sup>a</sup>Professor of Clinical Biostatistics and Medical Decision Making, Chair, Department of Biomedical Data Sciences, Leiden University Medical Center, Leiden, The Netherlands

<sup>b</sup>Professor of Medical Decision Making, Department of Public Health, Erasmus MC, Rotterdam, The Netherlands

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#### Abstract

Accurate prediction of medical outcomes is important for diagnosis and prognosis. The standard requirement in major medical journals is nowadays that validity outside the development sample needs to be shown. Is such data splitting an example of a waste of resources? In large samples, interest should shift to assessment of heterogeneity in model performance across settings. In small samples, cross-validation and bootstrapping are more efficient approaches. In conclusion, random data splitting should be abolished for validation of prediction models. © 2018 Elsevier Inc. All rights reserved.



<https://doi.org/10.1016/j.jclinepi.2015.04.005>

# The myth about data splitting for 'validation'

- **Inefficient** use of data (poorer model is developed)

Better solution for 'validation':

- For large samples: **Internal-external** validation
- For small samples: **Bootstrapping** or **cross-validation**

**Important note:** Machine learning approaches make use of data splitting methods (test and training) for internal optimization!

# External validation



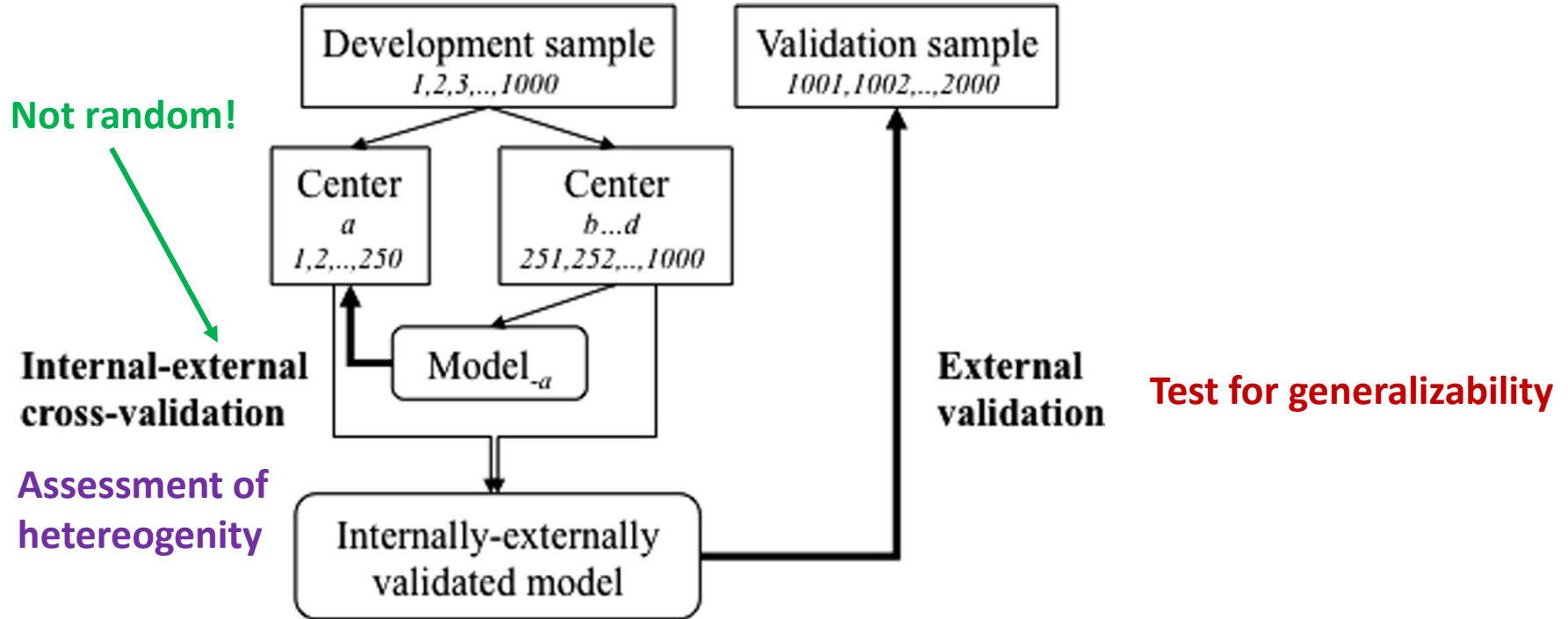
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Good model 'performance' in one study population **does not imply** good model performance in **new patients**

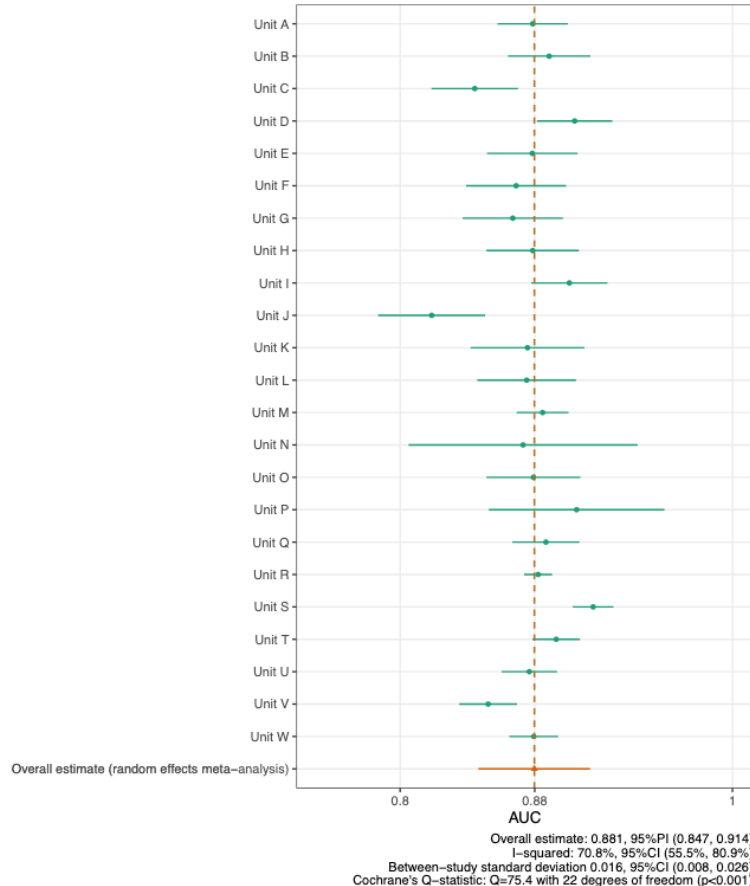
New patients = Patients from different centres, countries or times  
(different, but similar!)

# (Internal-)external validation



# (Internal-)external validation

**Supplemental Figure 8:** Geographic transportability: AUC random effects meta-analysis.



- We used a proposed framework for interpreting validation and transportability properties of prediction models and concluded that while our model showed good geographic discrimination transportability, other performance measures revealed a moderate to high heterogeneity between hospitals.



# Reasons for poor validity

*“There is no such that thing as a validated prediction model!”*

<https://doi.org/10.1186/s12916-023-02779-w>

- **Modelling aspects:** Small samples, overfitting, optimism
- **Population** differences, changes of over time
- **Definition, coding and assessment** of predictors/outcomes differ across hospitals and time

# Reasons for poor validity

“Rather, the current focus on developing new models **should shift to a focus on more extensive, well-conducted, and well-reported validation studies of promising models.”**

<https://doi.org/10.1186/s12916-023-02779-w>

# Some references

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Steyerberg et al.: **Assessing the performance of prediction models: a framework for traditional and novel measures.** Epidemiology. 2017 2010 Jan;21(1):128-38. doi: 10.1097/EDE.0b013e3181c30fb2

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